

FWI_Final_Stable_Version

August 11, 2021

```
[1]: %load_ext autoreload
      %autoreload 2
      %matplotlib inline

      import warnings
      warnings.filterwarnings('ignore')

      import numpy as np
      import matplotlib.pyplot as plt
      import scipy as sp
      import segyio
      import pylops
```

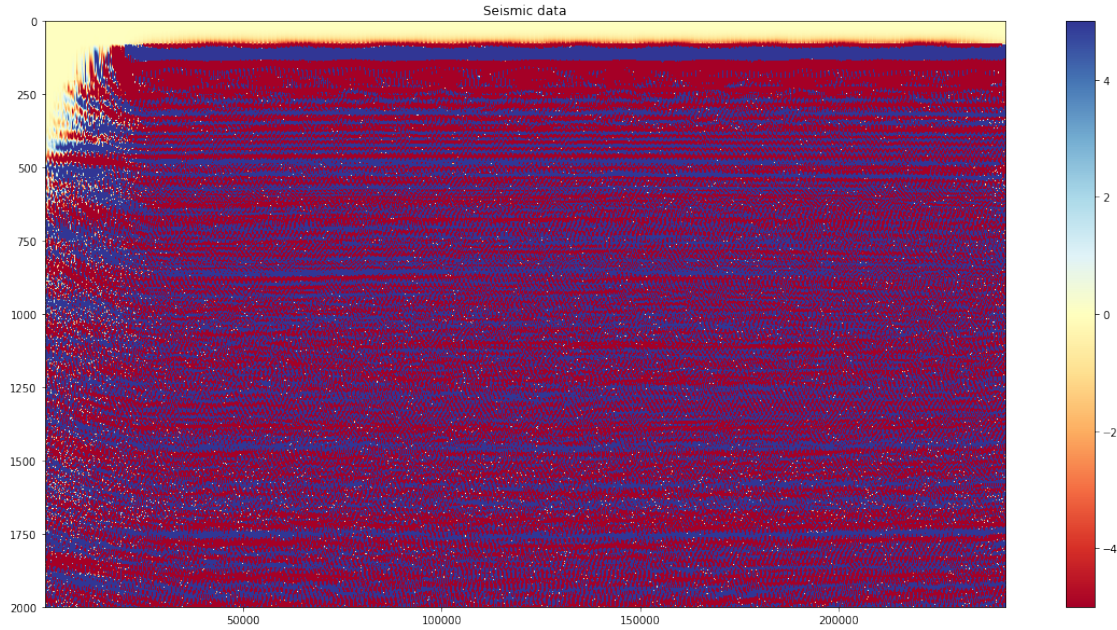
```
[2]: segyfile = '/home/tibo/sleipner/Sleipner_Seismic/p11ful/10p11ful.segy'

      f = segyio.open(segyfile, iline=seggyio.tracefield.TraceField.
      ↪SourceEnergyDirectionExponent,
      xline=seggyio.tracefield.TraceField.CDP)

      il, xl, t = f.ilines, f.xlines, f.samples
      dt = t[1] - t[0]

      d = segyio.cube(f)
      nil, nxl, nt = d.shape

      plt.figure(figsize=(20, 10))
      plt.imshow(d[nil//2].T, cmap='RdYlBu', vmin=-5, vmax=5,
      extent=(xl[0], xl[-1], t[-1], t[0]))
      plt.title('Seismic data')
      plt.colorbar()
      plt.axis('tight');
      plt.savefig('/home/tibo/sleipner/Sleipner_Seismic/seismic_data.png')
```



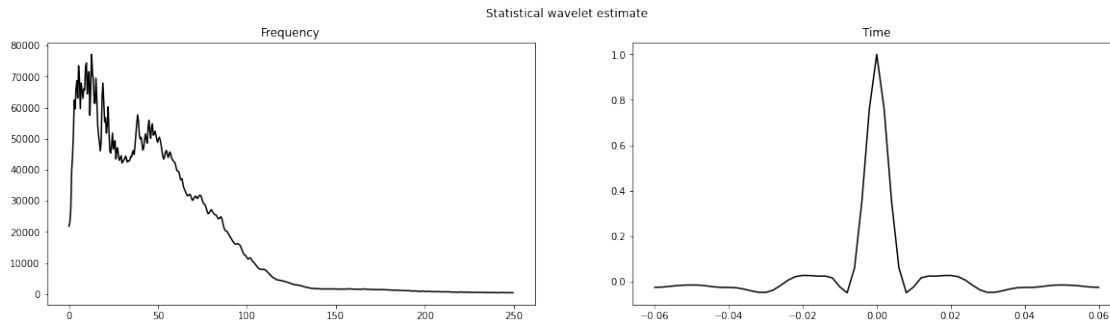
```
[3]: nt_wav = 31 # lenght of wavelet in samples
nfft = 2**10 # lenght of fft

# time axis for wavelet
t_wav = np.arange(nt_wav) * (dt/1000)
t_wav = np.concatenate((np.flipud(-t_wav[1:]), t_wav), axis=0)

# estimate wavelet spectrum
wav_est_fft = np.mean(np.abs(np.fft.fft(d[:, :500], nfft, axis=-1)), axis=(0,
→1))
fwest = np.fft.fftfreq(nfft, d=dt/1000)

# create wavelet in time
wav_est = np.real(np.fft.ifft(wav_est_fft)[:nt_wav])
wav_est = np.concatenate((np.flipud(wav_est[1:]), wav_est), axis=0)
wav_est = wav_est / wav_est.max()
wcenter = np.argmax(np.abs(wav_est))

# display wavelet
fig, axs = plt.subplots(1, 2, figsize=(20, 5))
fig.suptitle('Statistical wavelet estimate')
axs[0].plot(fwest[:nfft//2], wav_est_fft[:nfft//2], 'k')
axs[0].set_title('Frequency')
axs[1].plot(t_wav, wav_est, 'k')
axs[1].set_title('Time');
```



```
[4]: # swap time axis to first dimension
d_small = d[..., :200]
d_small = np.swapaxes(d_small, -1, 0)

m_relative, r_relative = \
    pylops.avo.poststack.PoststackInversion(d_small, wav_est, m0=np.
    ↪zeros_like(d_small), explicit=True, epsI=1e-4,
    simultaneous=False)

m_relative_reg, r_relative_reg = \
    pylops.avo.poststack.PoststackInversion(d_small, wav_est, m0=m_relative,
    ↪epsI=1e-4, epsR=1e0,
    **dict(iter_lim=10, show=2))

# swap time axis back to last dimension
d_small = np.swapaxes(d_small, 0, -1)
m_relative = np.swapaxes(m_relative, 0, -1)
m_relative_reg = np.swapaxes(m_relative_reg, 0, -1)
r_relative = np.swapaxes(r_relative, 0, -1)
r_relative_reg = np.swapaxes(r_relative_reg, 0, -1)
```

```
LSQR           Least-squares solution of  Ax = b
The matrix A has 96854400 rows and 48427200 columns
damp = 0.0000000000000000e+00   calc_var =      0
atol = 1.00e-08                 conlim = 1.00e+08
btol = 1.00e-08                 iter_lim =     10
```

	Itn	x[0]	r1norm	r2norm	Compatible	LS	Norm A	Cond A
	0	0.000000e+00	4.004e+06	4.004e+06	1.0e+00	8.7e-07		
	1	-1.76460e-04	1.400e+06	1.400e+06	3.5e-01	5.5e-01	3.7e+00	
1.0e+00								
	2	-2.93130e-04	1.001e+06	1.001e+06	2.5e-01	2.6e-01	4.8e+00	
2.1e+00								
	3	-3.48533e-04	8.515e+05	8.515e+05	2.1e-01	2.2e-01	5.5e+00	
3.5e+00								
	4	-3.53159e-04	7.216e+05	7.216e+05	1.8e-01	1.8e-01	6.3e+00	

5.4e+00	5	-2.89512e-04	6.588e+05	6.588e+05	1.6e-01	1.1e-01	7.1e+00
7.2e+00	6	-1.82346e-04	6.289e+05	6.289e+05	1.6e-01	8.4e-02	7.8e+00
8.8e+00	7	3.28588e-05	5.942e+05	5.942e+05	1.5e-01	8.6e-02	8.3e+00
1.1e+01	8	2.50253e-04	5.677e+05	5.677e+05	1.4e-01	5.9e-02	8.9e+00
1.4e+01	9	4.03195e-04	5.553e+05	5.553e+05	1.4e-01	4.7e-02	9.4e+00
1.6e+01	10	6.25561e-04	5.432e+05	5.432e+05	1.4e-01	4.8e-02	9.8e+00
1.8e+01							

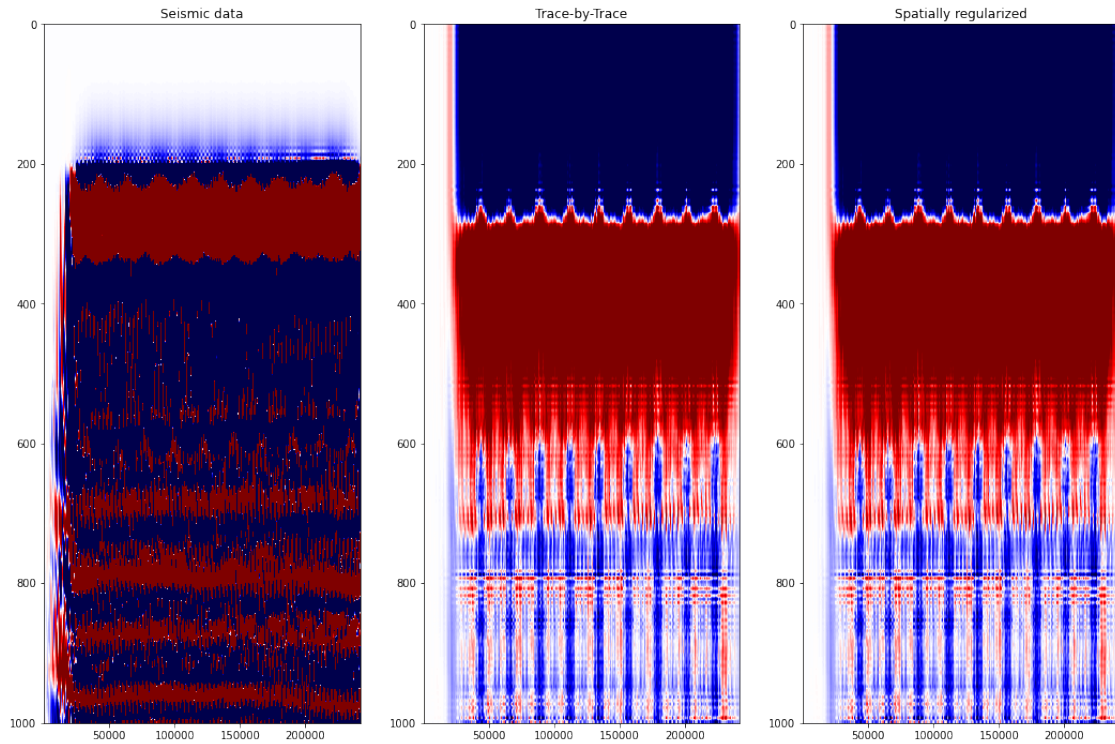
LSQR finished

The iteration limit has been reached

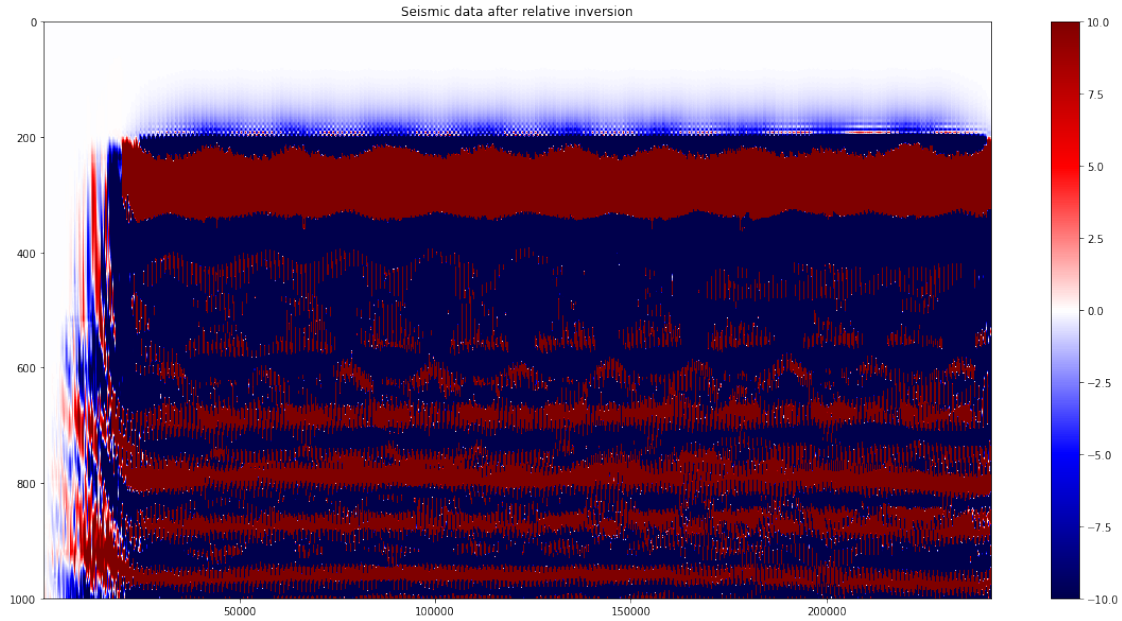
istop =	7	r1norm = 5.4e+05	anorm = 9.8e+00	arnorm = 2.5e+05
itn =	10	r2norm = 5.4e+05	acond = 1.8e+01	xnorm = 1.5e+06

```
[5]: fig, axs = plt.subplots(1, 3, figsize=(18, 12))
fig.suptitle('Relative inversion')
axs[0].imshow(d_small[nil//2].T, cmap='seismic', vmin=-10, vmax=10,
              extent=(xl[0], xl[-1], t[500], t[0]))
axs[0].set_title('Seismic data')
axs[0].axis('tight')
axs[1].imshow(m_relative[nil//2].T, cmap='seismic', vmin=-0.2*m_relative.max(),
              ↪vmax=0.2*m_relative.max(),
              extent=(xl[0], xl[-1], t[500], t[0]))
axs[1].set_title('Trace-by-Trace')
axs[1].axis('tight')
axs[2].imshow(m_relative_reg[nil//2].T, cmap='seismic', vmin=-0.2*m_relative.
              ↪max(), vmax=0.2*m_relative.max(),
              extent=(xl[0], xl[-1], t[500], t[0]))
axs[2].set_title('Spatially regularized')
axs[2].axis('tight');
```

Relative inversion



```
[6]: plt.figure(figsize=(20, 10))
plt.imshow(d_small[nil//2].T, cmap='seismic', vmin=-10, vmax=10,
           extent=(xl[0], xl[-1], t[500], t[0]))
plt.title('Seismic data after relative inversion')
plt.colorbar()
plt.axis('tight');
plt.savefig('/home/tibo/sleipner/Sleipner_Seismic/seismic_data_inversion.png')
```



```
[7]: fig, axs = plt.subplots(1, 3, figsize=(18, 12))
fig.suptitle('Relative inversion - residuals')
axs[0].imshow(d_small[nil//2].T, cmap='seismic', vmin=-10, vmax=10,
              extent=(xl[0], xl[-1], t[500], t[0]))
axs[0].set_title('Seismic data')
axs[0].axis('tight')
axs[1].imshow(r_relative[nil//2].T, cmap='seismic', vmin=-10, vmax=10,
              extent=(xl[0], xl[-1], t[500], t[0]))
axs[1].set_title('Trace-by-Trace')
axs[1].axis('tight')
axs[2].imshow(r_relative_reg[nil//2].T, cmap='seismic', vmin=-10, vmax=10,
              extent=(xl[0], xl[-1], t[500], t[0]))
axs[2].set_title('Spatially regularized')
axs[2].axis('tight');
```

Relative inversion - residuals

